



# Place Value, Sequences and Coordinates

## Vocabulary

sequence, step size, integer, decimal, power of 10, generate, describe, extend, linear, non-linear, constant, inconsistent, alternating, formula, formulae, coordinate, x-axis, y-axis, quadrant, term, algebra

L.O. Generate and describe number sequences.



\_\_\_\_\_ has £3462 in his bank account and receives £1000 every month from a rich uncle. Work out the new bank balances.

Every 6 months \_\_\_\_\_ gets a 5% saving bonus from the bank. How much is in the account after 6 months? 12 months? 18 months?

# L.O. Generate and describe number sequences.

**A**

Write the first six numbers in each sequence.

	Start at	Rule		Start at	Rule		Start at	Rule
1	4	+10	6	65	-7	11	26	+9
2	38	-2	7	15	+20	12	30	-3
3	7	+3	8	110	-11	13	$\frac{1}{2}$	$+\frac{1}{2}$
4	29	-4	9	21	+2	14	80	-5
5	0.5	+1	10	948	-101	15	25	+25

**B**

Complete these sequences by filling in the boxes. Write the rule each time.

- |    |                      |                      |                      |                      |                      |                      |                      |  |
|----|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|--|
| 1  | 44                   | 47                   | 50                   | 53                   | <input type="text"/> | <input type="text"/> | <input type="text"/> |  |
| 2  | 89                   | 85                   | 81                   | 77                   | <input type="text"/> | <input type="text"/> | <input type="text"/> |  |
| 3  | 115                  | 140                  | 165                  | 190                  | <input type="text"/> | <input type="text"/> | <input type="text"/> |  |
| 4  | 0.5                  | 0.6                  | 0.7                  | 0.8                  | <input type="text"/> | <input type="text"/> | <input type="text"/> |  |
| 5  | -2                   | -4                   | -6                   | <input type="text"/> | <input type="text"/> | <input type="text"/> | -14                  |  |
| 6  | 119                  | 114                  | <input type="text"/> | <input type="text"/> | <input type="text"/> | 94                   | 89                   |  |
| 7  | -9                   | -6                   | <input type="text"/> | <input type="text"/> | <input type="text"/> | 6                    | 9                    |  |
| 8  | $\frac{1}{5}$        | $\frac{2}{5}$        | $\frac{3}{5}$        | $\frac{4}{5}$        | <input type="text"/> | <input type="text"/> | <input type="text"/> |  |
| 9  | 5                    | 3                    | 1                    | <input type="text"/> | <input type="text"/> | <input type="text"/> | -7                   |  |
| 10 | 37                   | <input type="text"/> | 55                   | <input type="text"/> | 73                   | <input type="text"/> | 91                   |  |
| 11 | 366                  | 316                  | <input type="text"/> | 216                  | <input type="text"/> | <input type="text"/> | 66                   |  |
| 12 | <input type="text"/> | -15                  | -10                  | <input type="text"/> | <input type="text"/> | 5                    | 10                   |  |
| 13 | $1\frac{6}{7}$       | <input type="text"/> | $1\frac{2}{7}$       | 1                    | <input type="text"/> | <input type="text"/> | $\frac{1}{7}$        |  |
| 14 | <input type="text"/> | <input type="text"/> | 4.5                  | 5                    | <input type="text"/> | 6                    | 6.5                  |  |
| 15 | <input type="text"/> | 182                  | <input type="text"/> | 380                  | <input type="text"/> | 578                  | 677                  |  |
| 16 | 10                   | 6                    | <input type="text"/> | <input type="text"/> | <input type="text"/> | -10                  | -14                  |  |

**C**

Copy these sequences and write the next three numbers. What is the rule for each sequence?  
Can you write the rule for the  $n$ th term?

**1** 84 72 60 48

**2** 64 71 78 85

**3** 1.1 1.07 1.04 1.01

**4** 4  $3\frac{5}{8}$   $3\frac{2}{8}$   $2\frac{7}{8}$

**5** 165 146 127 108

**6** -9 -7 -5 -3

**7** 75 67 59 51

**8** 0.02 0.04 0.06 0.08

**9** 15 11 7 3

**10** 43 55 67 79

**11** -20 -14 -8 -2

**12** 5 4.5 4 3.5

**13** 135 156 177 198

**14** 36 28 20 12

**15** 50 175 300 425

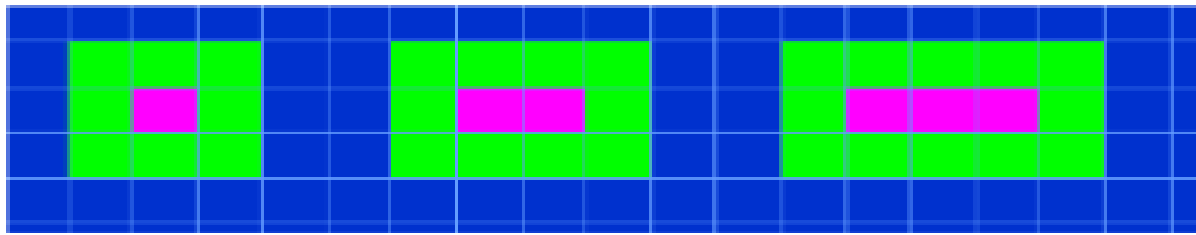
**16** 1.25 1.5 1.75 2

**17** 10  $8\frac{3}{4}$   $7\frac{1}{2}$   $6\frac{1}{4}$

**18** -11 -8 -5 -2



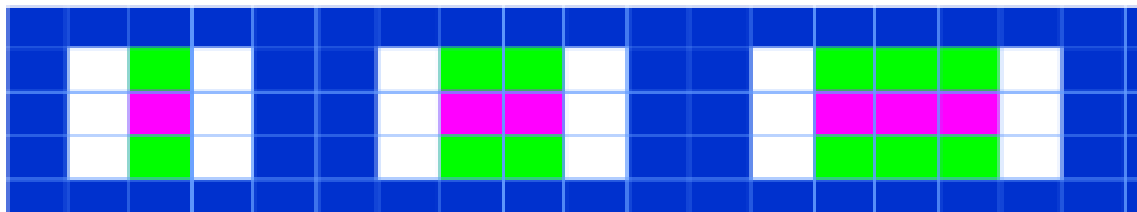
## Cows in a Field



- One cow [pink/centre square] needs to be kept in a field – green squares. Hence one cow needs 8 pieces of fence to stay in the field.

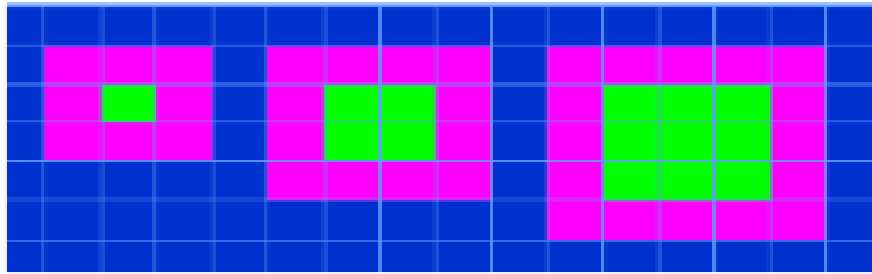
*What if there were 128 cows? Is there a rule?*

- What is the same in each 'field' even though they have a different number of cows in them?



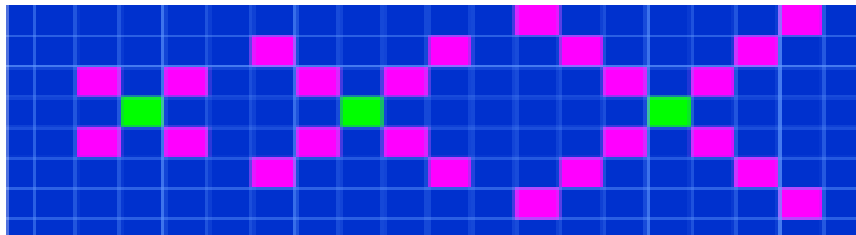
- Does this help to predict how many pieces of fence is required for 128 cows?

**Window Frames** – what length of frame would be required for a window that was 60 x 60?



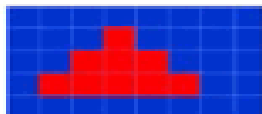
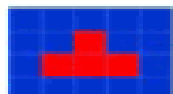
### Cross Patterns

How many squares would be in the 12<sup>th</sup> cross in the sequence?



### Stairs

The first stair is made from one square, the second from adding a row of 3 more, giving a total of 4. The next in the sequence would have a row of 5 added requiring a total of 9. What is the next 3 in the sequence? What would the  $n$ th stair look like?



# ANSWERS

## A

- |                           |  |
|---------------------------|--|
| 1 4 14 24 34 44 54        | 9 21 23 25 27 29 31                                  |
| 2 38 36 34 32 30 28       | 10 948 847 746 645 544 443                           |
| 3 7 10 13 16 19 22        | 11 26 35 44 53 62 71                                 |
| 4 29 25 21 17 13 9        | 12 30 27 24 21 18 15                                 |
| 5 0.5 1.5 2.5 3.5 4.5 5.5 | 13 $\frac{1}{2}$ 1 $1\frac{1}{2}$ 2 $2\frac{1}{2}$ 3 |
| 6 65 58 51 44 37 30       | 14 80 75 70 65 60 55                                 |
| 7 15 35 55 75 95 115      | 15 25 50 75 100 125 150                              |
| 8 110 99 88 77 66 55      |  |

## B

- |  |                       |
|--|-----------------------|
| 1 ... 56 59 62   | (add 3)               |
| 2 ... 73 69 65   | (take 4)              |
| 3 ... 215 240 265  | (add 25)              |
| 4 ... 0.9 1.0 1.1  | (add 0.1)             |
| 5 ... -8 -10 -12 -14   | (take 2)              |
| 6 ... 109 104 99 94 89   | (take 5)              |
| 7 ... -3 0 3 6 9   | (add 3)               |
| 8 ... $1\frac{1}{5}$ $1\frac{2}{5}$  | (add $\frac{1}{5}$ )  |
| 9 ... 5 3 1 -1 -3 -5 -7  | (take 2)              |
| 10 ... 37 46 55 64 73 82 91  | (add 9)               |
| 11 ... 366 316 266 216 166 116 66  | (take 50)             |
| 12 ... -20 -15 -10 -5 0 5 10   | (add 5)               |
| 13 ... $1\frac{6}{7}$ $1\frac{4}{7}$ $1\frac{2}{7}$ $1\frac{5}{7}$ $1\frac{3}{7}$ $1\frac{1}{7}$ | (take $\frac{2}{7}$ ) |
| 14 ... 3.5 4 4.5 5 5.5 6 6.5   | (add 0.5)             |
| 15 ... 83 182 281 380 479 578 677  | (add 99)              |
| 16 ... 10 6 2 -2 -6 -10 -14  | (take 4)              |

## C

- |  |                                |
|--|--------------------------------|
| 1 ... 36 24 12                                     | $96 - 12n$                     |
| 2 ... 92 99 106                                    | $7n + 57$                      |
| 3 ... 0.98 0.95 0.92                               | $1.13 - \frac{3n}{100}$        |
| 4 ... $2\frac{4}{8}$ $2\frac{1}{8}$ $1\frac{6}{8}$ | $4\frac{3}{8} - \frac{3n}{8}$  |
| 5 ... 89 70 51                                     | $184 - 19n$                    |
| 6 ... -1 1 3                                       | $2n - 11$                      |
| 7 ... 43 35 27                                     | $83 - 8n$                      |
| 8 ... 0.1 0.12 0.14                                | $\frac{2n}{100}$               |
| 9 ... -1 -5 -9                                     | $19 - 4n$                      |
| 10 ... 91 103 115                                  | $12n + 31$                     |
| 11 ... 4 10 16                                     | $6n - 26$                      |
| 12 ... 3 2.5 2                                     | $5.5 - \frac{5n}{10}$          |
| 13 ... 219 240 261                                 | $21n + 114$                    |
| 14 ... 4 -4 -12                                    | $44 - 8n$                      |
| 15 ... 550 675 800                                 | $125n - 75$                    |
| 16 ... 2.25 2.5 2.75                               | $\frac{n}{4} + 1$              |
| 17 ... $5\frac{3}{4}$ $2\frac{1}{2}$               | $11\frac{1}{4} - \frac{5n}{4}$ |
| 18 ... 1 4 7                                       | $3n - 14$                      |